

Optical Contrast: a Review and Application of Chi-Square Analysis

Ultrafast Laser Lab



Neema Rafizadeh

rafizadehn@ku.edu

March 26, 2022



- 1 Background to Optical Contrast.
- 2 Mathematical Introduction to Chi-Square Analysis.
- 3 Chi-Square Test on a Sample Set of Data.
- 4 Chi-Square Analysis for Platinum Diselenide (PtSe_2).
- 5 Future Plans.



Background

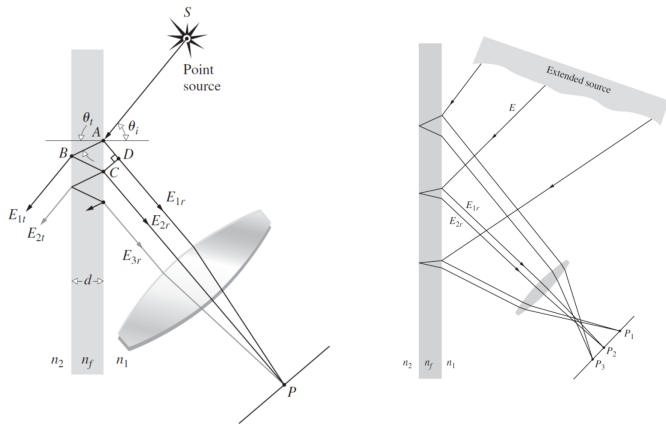


Figure 1: Optical path of light reflected off thin film.¹

¹Hecht, E. (2002). *Optics* (4th ed.). San Francisco, CA: Addison-Wesley.

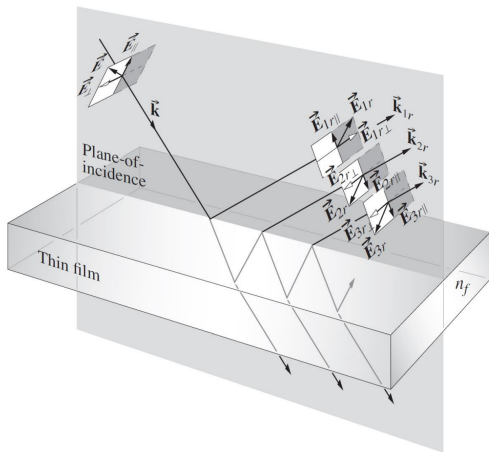


Figure 2: Phase shift of light reflected off thin film.²

²Hecht, E. (2002). *Optics* (4th ed.). San Francisco, CA: Addison-Wesley.

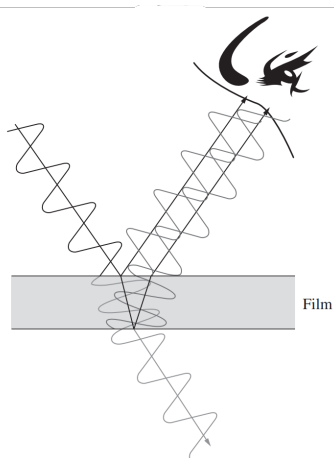


Figure 3: Overall representation of thin-film interference.³

³Hecht, E. (2002). *Optics* (4th ed.). San Francisco, CA: Addison-Wesley.



Figure 4: Oil spill of the Japanese bulk carrier *MV Wakashio*. ⁴

⁴Field, Rebecca. "Oil Is Leaking All over the World." Greenpeace International, 9 Apr. 2021.

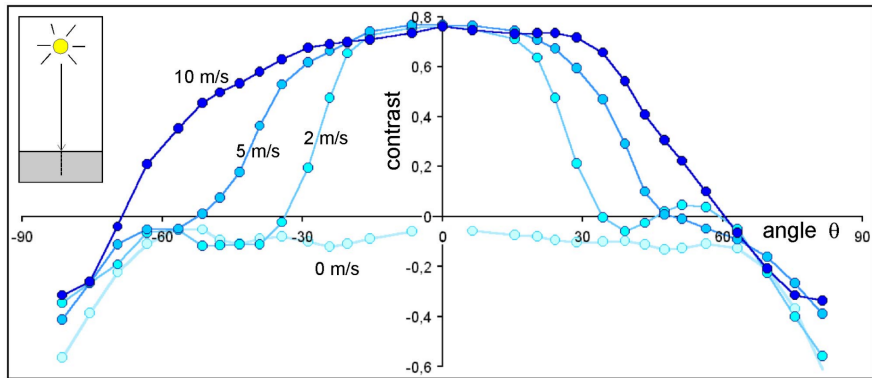


Figure 5: Contrast of an oil film using 550 nm incident light. ⁵

⁵Z. Otremba and J. Piskożub, "Modelling of the optical contrast of an oil film on a sea surface," *Opt. Express* **9**, 411-416 (2001).

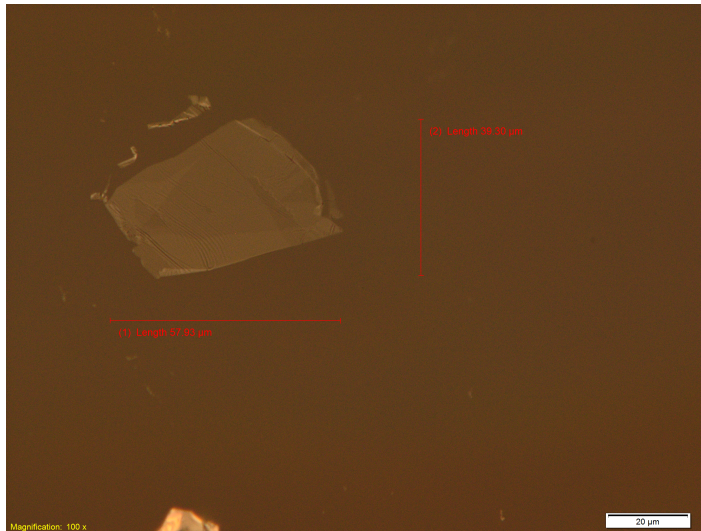


Figure 6: Example of graphene under optical microscope.

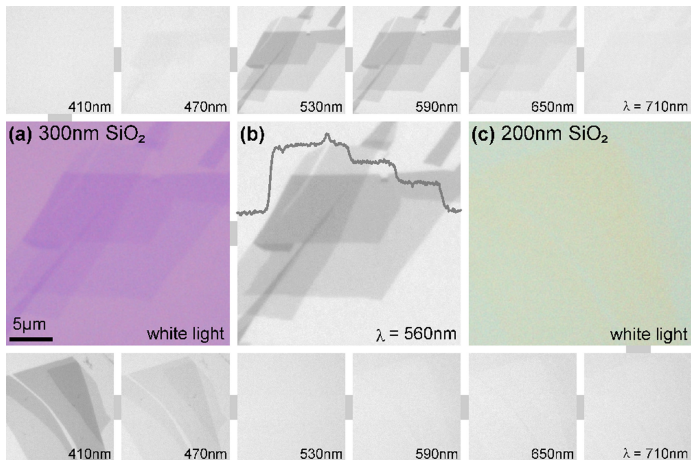


Figure 7: Optical contrast of few-layer graphene. ⁶

⁶Blake, P, et al. "Making Graphene Visible." *Applied Physics Letters* **91**, no. 6, 2007, pp. 063124–063124-3.

This is great because . . .

- no complicated sample preparation,
- can calculate the index of refraction of the thin material,
- can calculate the thickness of the thin material.

However, there is one problem.

What if I don't know the contrast of a monolayer of my material?



- 1 Background to Optical Contrast.
- 2 Mathematical Introduction to Chi-Square Analysis.
- 3 Chi-Square Test on a Sample Set of Data.
- 4 Chi-Square Analysis for Platinum Diselenide (PtSe_2).
- 5 Future Plans.

The standard equation for Chi-Square is given by,

General Chi-Square Equation

$$\chi^2 = \sum_{i=1}^N \frac{(O_i - E_i)^2}{E_i}$$

where O_i are the measured experimental values and E_i are the expected values from the applied fit.

Through this process, a chi-square test essentially measures **how well experimentally measured results compare to an applied fit.**



What Does Chi-Square Represent?

General Chi-Square Equation

$$\chi^2 = \sum_{i=1}^N \frac{(O_i - E_i)^2}{E_i}$$

Now, our specific analysis replaces the variables as,

Contrast-Specific Chi-Square Equation

$$\chi^2 = \sum_{i=1}^N \frac{(C_{i,\text{sample}} - n_i C_{i,1L})^2}{n_i C_{i,1L}} \quad \text{where} \quad n_i = \text{nint} \left(\frac{C_{i,\text{sample}}}{C_{i,1L}} \right)$$

Our **unknowns** are **the chi-square** and the **monolayer contrast**.

- 1 Background to Optical Contrast.
- 2 Mathematical Introduction to Chi-Square Analysis.
- 3 Chi-Square Test on a Sample Set of Data.**
- 4 Chi-Square Analysis for Platinum Diselenide (PtSe_2).
- 5 Future Plans.



Calculation of a Single Potential Value

Example of a Single Chi-Square Calculation

Let us use the set,

$$[8, 15, 16]$$

and see how well the integer 5 fits as their common multiple:

$$\begin{aligned}\chi^2 &= \sum_{i=1}^3 \frac{(O_i - E_i)^2}{E_i} \\ &= \frac{(8 - 10)^2}{10} + \frac{(15 - 15)^2}{15} + \frac{(16 - 15)^2}{15} \\ &\approx 0.5\end{aligned}$$

which demonstrates 5 may not be the best fit for this set of data.

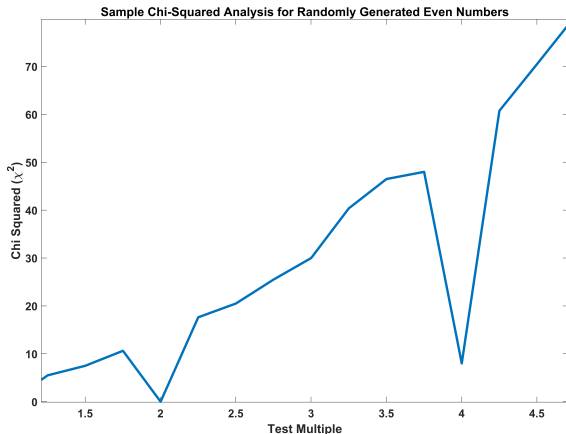


Figure 8: The graph here shows 2 as a much better fit for the integer multiple as the chi-squared value reaches 0, while the value for 4 is non-zero.



- 1 Background to Optical Contrast.
- 2 Mathematical Introduction to Chi-Square Analysis.
- 3 Chi-Square Test on a Sample Set of Data.
- 4 Chi-Square Analysis for Platinum Diselenide (PtSe_2).
- 5 Future Plans.



Figure 9: Example of one of the PtSe₂ flakes used to calculate contrast.

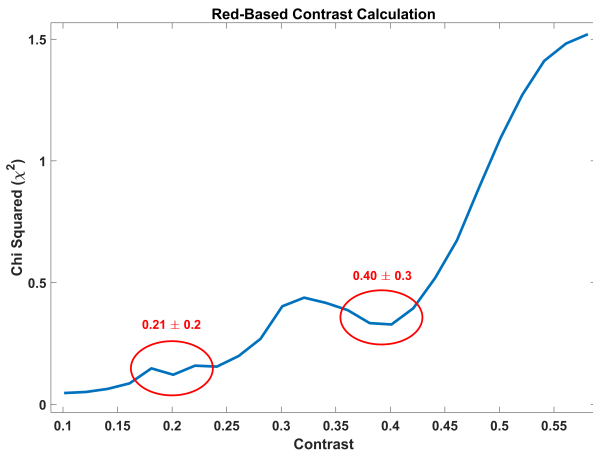


Figure 10: Chi-Square analysis of contrast data from roughly 40 flakes results in a conclusion of the monolayer having a contrast of 0.21 ± 0.2 .

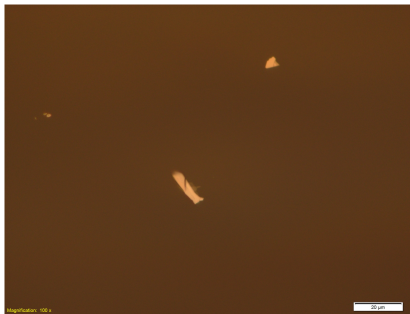


Figure 11: Monolayer found after calculating the chi-square predicted value, falls within reasonable contrast uncertainty from prediction.

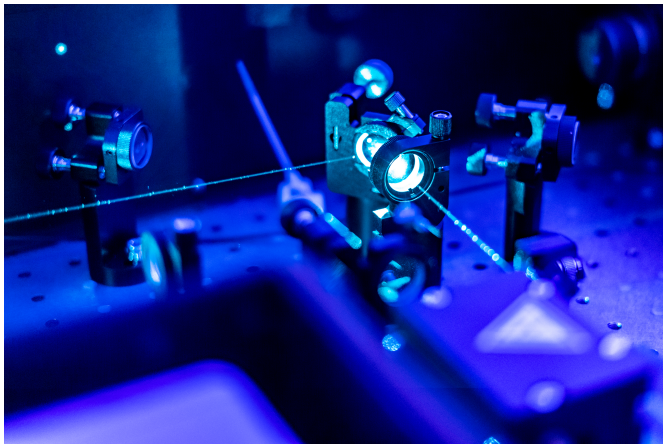


- 1 Background to Optical Contrast.
- 2 Mathematical Introduction to Chi-Square Analysis.
- 3 Chi-Square Test on a Sample Set of Data.
- 4 Chi-Square Analysis for Platinum Diselenide (PtSe_2).
- 5 Future Plans.



Future plans include:

- preparing an AFM-ready sample to verify calculated thickness.
- design a setup to verify calculated refractive index.



Fin.